STA 2023  Practice Questions  Final Exam

What you need to know:

General Format for Confidence Interval – estimator +/- (t or z) est. standard error

General Format of Test Statistic -- (t or z) = \( \frac{\text{estimator} - \# \text{ from } H_o}{\text{estimate of stderr}} \)

Table given to you on the test:

**STATISTICAL INFERENZE TABLE:**

<table>
<thead>
<tr>
<th>Case</th>
<th>parameter</th>
<th>estimator</th>
<th>standard error</th>
<th>Sampling Distribution</th>
</tr>
</thead>
<tbody>
<tr>
<td>one mean</td>
<td>( \mu )</td>
<td>( \bar{x} )</td>
<td>( \frac{s}{\sqrt{n}} )</td>
<td>t (n-1)</td>
</tr>
<tr>
<td>Mean of matched pairs dif.</td>
<td>( \mu_d )</td>
<td>( \bar{x}_d )</td>
<td>( \frac{s_d}{\sqrt{n}} )</td>
<td>t (n-1)</td>
</tr>
<tr>
<td>difference of two independent means</td>
<td>( \mu_1 - \mu_2 )</td>
<td>( \bar{x}_1 - \bar{x}_2 )</td>
<td>( \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} )</td>
<td>t with conservative df = smallest of (n1-1) and (n2-1)</td>
</tr>
<tr>
<td>one proportion</td>
<td>( p )</td>
<td>( \hat{p} )</td>
<td>CI: ( \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} )</td>
<td>z</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>ST: ( \sqrt{\frac{p_0(1-p_0)}{n}} )</td>
<td></td>
</tr>
<tr>
<td>difference of two independent proportions</td>
<td>( p_1 - p_2 )</td>
<td>( \hat{p}_1 - \hat{p}_2 )</td>
<td>CI: ( \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} )</td>
<td>z</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>ST: ( \sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)} )</td>
<td></td>
</tr>
</tbody>
</table>

McNemar \( TS = \frac{YN - NY}{\sqrt{YN + NY}} \) OR \( TS = \frac{NY - YN}{\sqrt{YN + NY}} \)
Questions 1 – 4  An education researcher has developed a new technique to teach Spanish to high school students. To prove this new method is better, she will teach two groups of students for an entire semester, one with the new method and one with the standard method used today in high schools. She wishes to obtain 12 sets of identical twins, 24 people total, and split the twins up so that one of each twin is in Class 1, which will receive the new technique, and one is in Class 2, which will receive the old technique. At the end of the semester both classes will take a standardized exam and the results will be compared.

1. What method should be used to analyze this data?
   a) one mean
   b) two independent means
   c) comparing means of dependent samples
   d) two independent proportions

2. What should our hypotheses be to test if your new method is better than the old method?
   a) \( H_0: \mu_1 - \mu_2 = 0 \) vs. \( H_A: \mu_1 - \mu_2 < 0 \)
   b) \( H_0: \mu_D = 0 \) vs. \( H_A: \mu_D < 0 \)
   c) \( H_0: \mu_1 - \mu_2 = 0 \) vs. \( H_A: \mu_1 - \mu_2 > 0 \)
   d) \( H_0: \mu_D = 0 \) vs. \( H_A: \mu_D > 0 \)

3. What distribution would you use to look up the p-value for this test of hypothesis?
   a) \( t(11) \)
   b) \( t(12) \)
   c) \( t(23) \)
   d) \( Z \)

4. Suppose we collect the data from this experiment and we find a p-value of 0.009. Which of the following is our conclusion at any reasonable alpha level?
   a) There is no statistically significant evidence of a difference among the two educational methods.
   b) There is evidence that the old method is better than the new method.
   c) There is evidence that the new method is better than the old method.
   d) We cannot determine without more information.
Questions 5-7 use the following modifications to the above scenario.
Unable to obtain the 12 sets of twins to conduct the experiment, the researcher has to use two existing Spanish classes at a local high school, one with 12 students and the other one with 11 students. Class 1 will receive the new technique and Class 2 will receive the old technique.

5. What method should be used to analyze this data?
   a) one mean  b) two independent means
   c) comparing means of dependent samples  d) two independent proportions

6. What should our hypotheses be to test if your new method is better than the old method?
   a) $H_0: \mu_1 - \mu_2 = 0$ vs. $H_A: \mu_1 - \mu_2 < 0$
   b) $H_0: \mu_D = 0$ vs. $H_A: \mu_D < 0$
   c) $H_0: \mu_1 - \mu_2 = 0$ vs. $H_A: \mu_1 - \mu_2 > 0$
   d) $H_0: \mu_D = 0$ vs. $H_A: \mu_D > 0$

7. What distribution would you use to look up the p-value for this test of hypothesis?
   a) t(11)  b) t(10)
   c) t(23)  d) Z

8. Find the t* value for a 99% confidence interval.
   a.) 3.169  b.) 2.576  c.) 3.250  d.) 2.821

Questions 9-11  We suspect that men are convicted of DUI (driving under the influence of alcohol or drugs) more often than women. Let $p_1$ be the proportion of males convicted of a DUI offense and $p_2$, the proportion of females convicted of a DUI offense.

9. If the 95% CI for $p_1 - p_2$ is (-.163, -.02). Which of the following can we conclude?
   a) There is evidence that males have a higher proportion of convictions for DUI than females.
   b) There is evidence that females have a higher proportion of convictions for DUI than males.
   c) There is no statistically significant evidence that there is a difference in the proportion of convictions for DUI for males and females.

10. Suppose we test $H_0: p_1 - p_2 = 0$ vs. $H_A: p_1 - p_2 \neq 0$. What can we say about the p-value?
    a) it is greater than .05  b) it is less than .05
    c) it is less than .025  d) cannot say anything about the p-value

11. Are there any problems with the assumptions necessary for these conclusions to be valid?
    a) The data may not have been randomly selected, and thus, not representative of the population.
    b) The sample sizes may not have been large enough for the formulas to be appropriate.
    c) There may be problems with both randomness and sample sizes.
    d) There are no problems with this data.
Questions 12 – 14  Many university courses require students to type their written assignments. Do students get better at typing because of this? Researchers want to see if incoming freshmen have a slower average typing rate (in words per minute) than graduating seniors. A random sample of 50 freshmen and 50 seniors was taken, and each was given a typing test to determine their typing rate. This data was entered into Minitab, and the results are shown below:

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>Freshmen</td>
<td>50</td>
<td>27.9</td>
<td>13.4</td>
<td>1.9</td>
</tr>
<tr>
<td>Seniors</td>
<td>50</td>
<td>34.0</td>
<td>12.5</td>
<td>1.8</td>
</tr>
</tbody>
</table>

95% CI for mu Freshmen - mu Seniors: ( -11.2, -0.9)
T-Test mu Freshmen = mu Seniors (vs <): T = -2.32  P = 0.011  DF = 97

12. Which of the following can we conclude from this output (at the 95% confidence level)?
   a) There is evidence that freshmen have a lower average typing rate than seniors.
   b) There is evidence that freshmen have a higher average typing rate than seniors.
   c) There is evidence that freshmen and seniors type at exactly the same rate, on average.
   d) There is no statistically significant evidence to show a difference between the mean typing rates of freshmen and seniors.

13. Which of the following statements are true?
   I. With a p-value equal to 0.011, we are confident that the mean typing rate for freshmen is smaller than the mean typing rate for seniors.
   II. The probability that the true mean difference for freshmen-seniors lies between -0.9 and -11.2 is .95.
   III. The probability that the mean typing rate of freshmen equals the mean typing rate of seniors is .011.

   a) Only I is true.
   b) Only III is true.
   c) Only I & II are true.
   d) All three statements are true.

14. Which of these are necessary assumptions when making inferences based on this data?
   I. Each sample is randomly drawn from the population
   II. The two samples are independent.
   III. Each population size is at least 10 times larger than the sample size from that population.

   a) Only I is assumed.
   b) Only III is assumed.
   c) Only I & II are assumed.
   d) All three are assumed.
Questions 15-20  Global warming has gotten a lot of media attention over the past few years, but researchers in Antarctica are keeping track of temperatures at the South Pole to try to see if temperatures really are rising. They know that from 1900-1999(last century) the average temperature at the South Pole was -6 degrees Celsius. They have randomly sampled 25 days from the past 2 years(this century) and collected the following data:

-6.0 -1.3 -2.4 -0.4 -3.4 2.1 -6.1 6.4 1.1 -4.2 -38.0 -0.1 0.5 -5.8 -3.5 2.8 -6.5 4.3 -1.5 -1.8 1.9 2.8 3.5 0.8 2.1

15. What are the appropriate $H_0$ and $H_a$ to use here?
   a) $H_0$: $\mu = -2.1$ \hspace{1cm} $H_a$: $\mu > -2.1$
   b) $H_0$: $\mu = -6$ \hspace{1cm} $H_a$: $\mu > -6$
   c) $H_0$: $\mu = -6$ \hspace{1cm} $H_a$: $\mu \neq -6$
   d) $H_0$: $\mu_1 - \mu_2 = 0$ \hspace{1cm} $H_a$: $\mu_1 - \mu_2 \neq 0$
   e) $H_0$: $\mu_1 - \mu_2 = 0$ \hspace{1cm} $H_a$: $\mu_1 - \mu_2 > 0$

16. What is the standard error?
   a) 8.26 \hspace{1cm} b) 8.09 \hspace{1cm} c) 1.618 \hspace{1cm} d) 1.652

17. What is the Test Statistic for this test?
   a) -4.9 \hspace{1cm} b) 3.89 \hspace{1cm} c) -1.28 \hspace{1cm} d) 2.35

18. Suppose the Test Statistic was 2.4. Then the p-value is between:
   a) .01 and .025 \hspace{1cm} b) .02 and .025
   c) .005 and .01 \hspace{1cm} d) .10 and .15

19. The 98% Confidence Interval obtained from this sample is (-5.99, 1.79). Based on this interval, which of the following statements are true? We are 98% confident that:
   (Be careful. Hint: What type of test is this?)
   a) the true mean temperature of this century is between 5.99 degrees lower and 1.79 degrees higher than the true mean temperature of last century at the South Pole.
   b) the true mean temperature of this century is between 5.99 degrees higher and 1.79 degrees lower than the true mean temperature of last century at the South Pole.
   c) the true mean temperature of this century is different than the true mean temperature of last century at the South Pole.
   d) the true mean temperature of this century is the same as the true mean temperature of last century at the South Pole.
   e) None of the above statements are true.

20. Which of the following problems cast doubts on our conclusions?
   a) The data was not randomly selected.
   b) The data is not representative of the whole century.
   c) The data does not seem to come from a Normal distribution.
   d) all of the above
   e) only a and b
   f) only b and c
   g) only a and c
Questions 21 – 23 Is left-handedness associated with gender in some way? Researchers were trying to determine if a connection could be made between the dominant hand and gender in high school students. They randomly sampled 1417 high school students across the country and obtained the following data:

<table>
<thead>
<tr>
<th></th>
<th>Male Students(1)</th>
<th>Female Students(2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Left Handed Students</td>
<td>68</td>
<td>97</td>
</tr>
<tr>
<td>Right Handed Students</td>
<td>545</td>
<td>707</td>
</tr>
</tbody>
</table>

21. What is the population of interest here?
   a) all left-handed high school students in the country
   b) all right-handed high school students in the country
   c) all male high school students in the country
   d) all female high school students in the country
   e) all high school students in the country

22. The 95% CI was (-0.0430, 0.0242) What can we conclude about the proportions of left handed students among male and female high school students at the 95% confidence level?
   a) There is evidence that the true proportion of male students that are left handed is higher than the true proportion of female students that are left handed.
   b) There is evidence that the true proportion of male students that are left handed is lower than the true proportion of female students that are left handed.
   c) There is evidence that the true proportion of male students that are left handed is equal to the true proportion of female students that are left handed.
   d) We cannot conclude that the true proportion of male students that are left handed is different from the true proportion of female students that are left handed.

23. Which of the following assumptions, necessary for the validity of this test, we suspect was violated in this case?
   a) data may not have been randomly selected
   b) males and females are not independent
   c) samples were too small
   d) none seems to be violated
Questions 24-27  Below is data collected from a random sample of 3,647 American professionals from 10 urban cities. We would like to know if male professionals(1) are more likely to have children than female(2) professionals of the same age (33-38).

<table>
<thead>
<tr>
<th></th>
<th>WOMEN Without children</th>
<th>WOMEN With children</th>
<th>MEN Without children</th>
<th>MEN With children</th>
<th>TOTALS Without children</th>
<th>TOTALS With children</th>
</tr>
</thead>
<tbody>
<tr>
<td>18-25</td>
<td>265</td>
<td>62</td>
<td>132</td>
<td>164</td>
<td>397</td>
<td>226</td>
</tr>
<tr>
<td>26-32</td>
<td>408</td>
<td>216</td>
<td>178</td>
<td>397</td>
<td>583</td>
<td>613</td>
</tr>
<tr>
<td>33-38</td>
<td>276</td>
<td>412</td>
<td>86</td>
<td>563</td>
<td>362</td>
<td>978</td>
</tr>
<tr>
<td>39-45</td>
<td>89</td>
<td>294</td>
<td>23</td>
<td>275</td>
<td>112</td>
<td>569</td>
</tr>
<tr>
<td>46+</td>
<td>23</td>
<td>145</td>
<td>64</td>
<td>455</td>
<td>87</td>
<td>600</td>
</tr>
</tbody>
</table>

24. This would be best analyzed as a:
   a) comparing means of dependent samples  b) One proportion
   c) Two independent means       d) Two independent proportions

25. Which data from the table above would we be analyzing in this case?
   a) all women vs. all men
   b) women aged 33-38 vs. men aged 33-38
   c) women aged 33-38 vs. totals for all people 33-38
   d) women aged 33-38 with children vs. women aged 33-38 without children

26. Are there any problems with this data that would violate the assumptions?
   a) Yes, there is an outlier.
   b) Yes, all the counts are too large.
   c) Yes, the data does not come from a Normal distribution.
   d) No problems.

Minitab gave the following output for this analysis.

95% CI for p(1) - p(2): (0.206951, 0.297170)
Test for p(1) - p(2) = 0 (vs > 0): Z = 10.95  P-Value = 0.000

27. What conclusion can we make about professional men and women, aged 33-38, in urban cities?
   a) There is not enough statistically significant evidence to conclude that professional men are more likely than professional women in this age group to have children.
   b) There is evidence that the proportion of professional men who have children is different than the proportion of professional women in this age group.
   c) There is evidence that the professional men are significantly more likely to have children than professional women in this age group.
   d) There is evidence that professional women are significantly more likely to have children than professional men in this age group.
28. An August 1999 ABC news poll of 506 Americans found that 4% of Americans cited “to go further in space” as their top priority for the new millennium, while 2% said “eliminate world hunger.” The 95% confidence interval for the difference in proportions was (-0.00098, 0.04098) What can we conclude?
   a) There is not enough statistically significant evidence to prove that more Americans support space advances than a solution to world hunger.
   b) The proportion of people in the population who support space advances and a solution to world hunger is exactly the same.
   c) We are 95% confident that more Americans support space advances than a solution to world hunger.
   d) We are 95% confident that more Americans support a solution to world hunger than space advances.

Questions 29-35 Which case is it? You can use each answer more than once.
   a) one mean
   b) one proportion
   c) matched pairs with means
   d) two independent means
   e) two independent proportions

29. A manufacturer of nails is interested in determining if their nails are meeting specifications. A sample of 100 nails was taken. Is the average length of the nails longer than 3 inches?

30. A sociologist suspects that members of pairs of heterosexual siblings of the same gender (brother-brother or sister-sister) get married at earlier ages on average than siblings who come from mixed-gender (brother-sister) pairs.

31. Does pesticide X affect the yield (in lbs) of any of 10 different varieties of tomatoes? Two fields (one treated and one untreated) are planted with 2 rows each of 10 varieties of tomatoes, and their yields are compared.

32. A gourmet pet food shop owner wants to estimate how many of his customers would continue to shop with him if he moved across town. He asks a random 50 shoppers if they’d drive across town to shop with him, and he makes a confidence interval to help make the decision to move or not.
33. The migration of African buffalo herds might be affected by the weight of the transponder used to track them. Last year, the scientists tried their standard transponder on eight herds of buffalo and recorded how far each group traveled. This year they will swap out the heavy transponders with more expensive, lighter ones and see if the same buffalo herds travel farther than last year.

34. A political action group wonders if college graduates are more likely to support increased penalties for repeat offenders than are those without college degrees.

35. Is the ice-cream cup filling machine accurate or not? A random sample of 20 quarts of ice cream is taken to see if the average contents is 247 mL of product.

36. Does eating breakfast improve productivity? In a Guess jeans factory, the workers of one sewing crew of 20 are fed a hearty breakfast for a month and then the same sewing crew of 20 is asked to go without eating until lunch time for another month. The teams’ productivity is compared for the two months.

37. Equal rights activists claim that, if admissions into a college’s architecture program are fair, half of all students admitted should be female. To test this hypothesis, they look at admissions data from 1982 (before aggressive recruiting of women) and 2001, asking “Has the proportion of women admitted changed significantly in the last decade?”

General Questions

38. When are p-values negative?
   a) when the test statistic is negative.
   b) when the sample statistic is smaller than the hypothesized value of the parameter
   c) when the confidence interval includes only negative values
   d) when we fail to reject the null hypothesis
   e) never

39. When can we decide to fail to reject the null hypothesis by looking at a confidence interval?
   a) when the interval includes only negative values
   b) when the interval includes only positive values
   c) when the interval includes both positive and negative values
   d) when the interval includes the hypothesized value of the parameter
   e) never
Questions 39 - 42  Two UF students are investigating how long it takes shoppers to find parking spaces at the Publix in Butler Plaza on different days of the week. To collect data, they position themselves at the parking lot entrance closest to Publix and, using a stopwatch, they record how long (in minutes) it takes every fifth car to come to a complete stop in a parking space. “Parkwkda” regards data collected on a weekday; “Parksat” on Saturday, and “Parkgame” on a Saturday which was also a UF football game day. NOTE: Minitab output appears on the following page. Some are relevant to this question, and some are not. Read them carefully.

40. How long, on average, does it take those in the sample to find a parking space on a weekday?
   a) 0.935 minutes
   b) 0.395 minutes
   c) 0.740 minutes
   d) cannot be determined from the information given

41. Does it take longer to find a parking space on Saturday than on a weekday? This should be analyzed as:
   a) two independent means
   b) two independent proportions
   c) comparing means of dependent samples

42. What can we conclude about the time it takes to find a parking space on Saturday compared to a weekday?
   a) The pvalue for this significance test is .23, which means there is not enough statistically significant evidence to prove a significant difference between these two times.
   b) The pvalue for this significance test is .33, which means there is not enough statistically significant evidence to prove a significant difference between these two times.
   c) The pvalue for this significance test is .0005, which means that there is evidence that it takes longer on a Saturday to find a parking space.
   d) The pvalue for this significance test is .002, which means that there is evidence that the time to find a space on Saturday is different than on a weekday.

43. Does it take longer to find a parking space on a Saturday than on a game day? This should be analyzed as:
   a) two independent means
   b) two independent proportions
   c) comparing means of dependent samples
44. What can we conclude about the time it takes to find a parking space on a Saturday compared to a game day?
   a) The p-value for this significance test is .23, which means there is not enough statistically significant evidence to prove a significant difference between these two times.
   b) The p-value for this significance test is .33, which means there is not enough statistically evidence to prove a significant difference between these two times.
   c) The p-value for this significance test is .0005, which means that there is evidence that it takes longer on a game day than on a Saturday to find a parking space.
   d) The p-value for this significance test is .002, which means that there is evidence that the time to find a space on a game day is different than on a Saturday.

Two Sample T-Test and Confidence Interval
Two sample T for parkwkday vs parksat

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>parkwkda</td>
<td>20</td>
<td>0.395</td>
<td>0.307</td>
<td>0.069</td>
</tr>
<tr>
<td>parksat</td>
<td>20</td>
<td>0.935</td>
<td>0.583</td>
<td>0.13</td>
</tr>
</tbody>
</table>

95% CI for mu parkwkda - mu parksat: ( -0.842, -0.24)
T-Test mu parkwkda = mu parksat (vs <): T = -3.66  P = 0.0005  DF = 28

Paired T-Test and Confidence Interval
Paired T for parkwkday - parksat

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>parkwkda</td>
<td>20</td>
<td>0.395</td>
<td>0.307</td>
<td>0.069</td>
</tr>
<tr>
<td>parksat</td>
<td>20</td>
<td>0.935</td>
<td>0.583</td>
<td>0.130</td>
</tr>
<tr>
<td>Difference</td>
<td>20</td>
<td>-0.540</td>
<td>0.678</td>
<td>0.152</td>
</tr>
</tbody>
</table>

95% CI for mean difference: (-0.857, -0.223)
T-Test of mean difference = 0 (vs not = 0): T-Value = -3.56  P-Value = 0.002

Two Sample T-Test and Confidence Interval
Two sample T for parksat vs parkgameday

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>parksat</td>
<td>20</td>
<td>0.935</td>
<td>0.583</td>
<td>0.13</td>
</tr>
<tr>
<td>parkgame</td>
<td>20</td>
<td>0.740</td>
<td>0.421</td>
<td>0.094</td>
</tr>
</tbody>
</table>

95% CI for mu parksat - mu parkgame: ( -0.13, 0.522)
T-Test mu parksat = mu parkgame (vs not =): T = 1.21  P = 0.23  DF = 34

(Continued onto the next page.)
Paired T-Test and Confidence Interval
Paired T for parksat - parkgameday

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>parksat</td>
<td>20</td>
<td>0.935</td>
<td>0.583</td>
<td>0.130</td>
</tr>
<tr>
<td>parkgameday</td>
<td>20</td>
<td>0.740</td>
<td>0.421</td>
<td>0.094</td>
</tr>
<tr>
<td>Difference</td>
<td>20</td>
<td>0.195</td>
<td>0.879</td>
<td>0.197</td>
</tr>
</tbody>
</table>

95% CI for mean difference: (-0.217, 0.607)
T-Test of mean difference = 0 (vs not = 0): T-Value = 0.99  P-Value = 0.33
45. Which of the following is TRUE?
a) For the method of two independent means, the size of the two samples can be different.
b) Matched pairs design uses the standard normal distribution, since the population is required to be normal.
c) The method of two independent means can be used for categorical response variables, whereas matched pairs design cannot.
d) All of the above.

46. Which of the following is TRUE?
a) Matched pairs design benefits from the fact that potential sources of bias are controlled.
b) The degrees of freedom for two independent means tests is $n_1 + n_2 - 1$.
c) We can use the normal distribution to find the p-value with comparing proportions from two independent samples because the data comes from a normal distribution.
d) All of the above.

Questions 47 – 49

According to a study in 2005 by American Research Group, an American adult spends on average an amount of $942 on gifts for the Christmas holiday. We claim that students at UF are likely to spend less than that amount. To test this claim, we randomly surveyed 25 students across campus, the resulted sample mean is 820.24, and the standard deviation is 260.4.

47. Which of the following hypothesis is correct?
a) $H_0: \mu = 942, \quad H_a: \mu < 942.$
b) $H_0: \mu = 0, \quad H_a: \mu \neq 0.$
c) $H_0: \mu = 942, \quad H_a: \mu > 942.$
d) $H_0: \mu = 942, \quad H_a: \mu \neq 942.$

48. Conduct the significant test, what is the value of the test statistic?
a) -2.338
b) 2.338
c) -0.468
d) 0.468

49. What is the associated p-value?
a) $0.01 < p\text{-value} < 0.025$
b) $0.02 < p\text{-value} < 0.05$
c) $0.005 < p\text{-value} < 0.0125$
d) $p\text{-value} = 0.0096$
50. A public health clinic administers a survey that addresses patient satisfaction with services. The survey uses a summary score on a 70 point scale, with 70 indicating the highest possible satisfaction. The survey instrument has been tested in other environments and has historically had mean \( \mu = 50 \).

We seek evidence that this population has mean score \( \mu \) that is less than 50 and take a SRS of \( n = 100 \). Suppose this sample gives a mean score of 48.4 and a standard deviation \( s = 7.5 \).

What is the p-value for this test?
   a. Between .05 and .025
   b. Between .025 and .1
   c. .0166
   d. None of the above

51. Lithium carbonate is a drug used to treat bipolar mental disorders. The average dose in well-maintained patients is \( \mu = 1.3 \) mEq/L. A random sample of 25 patients on lithium demonstrates a mean lithium level \( \bar{X} \) of 1.4 mEq/L and a standard deviation \( s= 0.3 \) mEq/L. Conduct a one sample t-test to see if the observed difference is significant. Use a two-sided alternative, as improper dosing would include both under- and over-dosing. What is the p-value for this test?
   a. Between .05 and .01
   b. Between .1 and .2
   c. Between .05 and .1
   d. Between .01 and .025
   e. None of the above

52. A test of \( H_0: \mu = 110 \) vs. \( H_a: \mu \neq 110 \) based on \( n = 18 \) gives \( t_{stat} = 2.11 \). What is the p-value for this problem?
   a. .05
   b. .025
   c. Between .05 and .1
   d. Between .01 and .025
   e. None of the above

53. A sample of birth weights (grams) of infants who had died of Sudden Infant Death Syndrome (SIDS) in a large metropolitan area was \{2998, 3740, 2031, 2804, 2454, 2780, 2203, 3803, 3948, 2268\}. The mean weight of all births in this metropolitan was 3300 grams. What are the degrees of freedom associated with the one-sample t-test of whether the mean birth weight of SIDS cases is significantly different from that of the rest of the population? (Two-sided test.)
   a. 11
   b. 10
   c. 9
   d. None of the above
54. Suppose a study to determine if the height of male athletes is larger than the average male height believed to be 70 inches was performed on a sample of 100 athletes. The p-value for this test is .003. Which one of these statements is true?
   a. We reject the null hypothesis at the $\alpha = 0.1, 0.05$, but not at the 0.01 level
   b. There is a 0.3% probability that we observe a test statistic as this high or more, assuming the null hypothesis is true
   c. 99.7% of the male athletes from the sample are taller than 70 inches
   d. 99.7% of male athletes in general are taller than 70 inches
   e. There is a 0.3% probability that we observe as high a test statistic as this assuming the null hypothesis is false

Questions 55 -56 The drying time of a certain type of paint under specified conditions is normally distributed with mean 75min. Chemists have proposed a new additive designed to reduce the average drying time. It is believed that drying times will remain normally distributed. The hypotheses to be tested are Ho: $\mu = 75$ versus Ha: $\mu < 75$. Experimental data from a random sample of 25 test specimens provided an estimate of 9 for the standard deviation.

55. What is the test statistic?
   a) $t = \frac{x + 75}{9/\sqrt{25}}$
   b) $t = \frac{x - 75}{9/\sqrt{25}}$
   c) $t = \frac{x + 9}{75/\sqrt{25}}$
   d) $t = \frac{9/\sqrt{25}}{75 - x}$

56. If the test statistic is equal to -2.80, for what values of $\alpha$ (probability of Type I error) would we reject Ho?
   a) 0.10
   b) 0.05
   c) 0.01
   d) All of the above
Questions 57-59 A random sample of 31 students were asked two questions:

- What is your gender? Male (1) or Female (2).
- How much money in dollars did you spend on textbooks this semester?

The Minitab output looks like:

<table>
<thead>
<tr>
<th></th>
<th>N</th>
<th>Mean</th>
<th>StDev</th>
<th>SE Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>17</td>
<td>325</td>
<td>116</td>
<td>28</td>
</tr>
<tr>
<td>2</td>
<td>14</td>
<td>263.9</td>
<td>64.4</td>
<td>17</td>
</tr>
</tbody>
</table>

95% CI for μ₁ - μ₂: (-7, 129)
T-Test μ₁ = μ₂ (Vs not =): T = 1.85  P = 0.076  DF = 25

57. What hypotheses are being tested? Let μ denote the mean for book expenditure.

a) Ho: μ₁-μ₂≠0 versus Ha: μ₁-μ₂=0
b) Ho: μ₁-μ₂=0 versus Ha: μ₁-μ₂<0
c) Ho: μ₁-μ₂=0 versus Ha: μ₁-μ₂≠0
d) Ho: μ₁-μ₂≤0 versus Ha: μ₁-μ₂>0

58. What test is being used?

a) 1-sample t-test .
b) McNemar.
c) paired t-test.
d) 2-sample t-test.

59. At what significance level can we reject the Ho?

a) At α=0.01 but not at α=0.10.
b) At α=0.05 but not at α=0.10.
c) At all α=0.01 α=0.05 α=0.10
d) A α=0.10 but not at α=0.05.
e) None of the above.
Questions 60 and 61: A researcher at a local university wants to find out the relationship between person’s height right before sleep and right after sleep. She asks 50 people, randomly selected, to participate in the study. These people monitor their heights for three days. Every night, right before the participants go to sleep, they measure their height and then sleep for approximately eight hours. After they wake up, they measure their height again, and take the difference between the measurements:

\[
\text{Difference} = \text{Height After Sleep} - \text{Height Before Sleep}
\]

This routine is performed for three consecutive nights and three differences are obtained. Finally, the differences are averaged to obtain an average difference, D, between heights. The researcher is using the following hypothesis test in her study:

\[
\begin{align*}
\text{Ho}: & \quad \mu_D = 0 \\
\text{Ha}: & \quad \mu_D > 0
\end{align*}
\]

60. What is the researcher trying to show using the above hypothesis test?
(a) People, on average, are taller after sleep than before sleep
(b) People, on average, are shorter after sleep than before sleep
(c) There is a difference between people’s average height before and after sleep
(d) There is no difference between people’s average height before and after sleep

61. If the p-value for the above hypothesis test is 0.21, what conclusion can we make, with \( \alpha \) being the usual 0.05?
(a) There is evidence that people, on average, are taller after sleep than before sleep
(b) There is evidence that people, on average, are shorter after sleep than before sleep
(c) There is no statistically significant evidence of a difference between people’s average height before and after sleep
(d) There is definitely no statistically significant evidence of a difference between people’s average height before and after sleep

Questions 62 – 63 After finishing her study of people’s heights, the researcher finds an article about the relationship between people’s weight before and after sleep. The article describes a study done at one of the universities, where an interesting result has been found. Based on the result described in the article, she wants to test whether students at her university weigh less after night’s sleep. Each student is weighed before and after sleeping.

62. Based on researcher’s goal, what could be the possible null hypothesis of her hypothesis test?
(a) People weigh more on average after sleep
(b) People weigh less on average after sleep
(c) There is evidence of a difference between the people’s average weight before and after sleep
(d) There is no statistically significant evidence of a difference between people’s average weight before and after sleep
63. If the p-value for the test conducted by the researcher is 0.003, \( \alpha \) equal to 0.05, what can be said about the conclusion of the test?
(a) There is evidence that students at her university weigh more after sleep than before sleep
(b) There is evidence that students at her university weigh less after sleep than before sleep
(c) There is evidence that students at her university weigh the same before and after sleep
(d) There is evidence that students at her university have different weight before and after sleep
(e) No conclusion can be drawn from the obtained p-value

64. In the problem described for questions 62/63 and for 60/61, what types of analysis were we performing?
(a) Both tests were comparisons of two independent proportions
(b) Both tests were comparisons of two independent means
(c) Both tests were comparisons of two dependent means
(d) The first test was comparison of independent proportions and the second was comparison of independent means
(e) The first test was comparison of independent means and the second was comparison of dependent means

Questions 65 – 69 In some mining operations, a byproduct of the processing is mildly radioactive. Of prime concern is the possibility that release of these byproducts into the environment may contaminate the freshwater supply. There are strict regulations for the maximum allowable radioactivity in supplies of drinking water, namely an average of 5 picocuries per liter (pCi/L) or less. However, it is well known that even safe water has occasional hot spots that eventually get diluted, so samples of water are assumed safe unless there is evidence to the contrary. A random sample of 25 specimens of water from a city's water supply gave a mean of 5.39 pCi/L and a standard deviation of 0.767 pCi/L.

65. What is the Hypothesis?
   a) Ho: \( \mu = 5.39 \), Ha: \( \mu \neq 5 \)
   b) Ho: \( \mu = 5 \), Ha: \( \mu \neq 5 \)
   c) Ho: \( \mu = 5.39 \), Ha: \( \mu \neq 5.39 \)
   d) Ho: \( \mu = 5.39 \), Ha: \( \mu \neq 5 \)
   e) Ho: \( \mu = 5 \), Ha: \( \mu \neq 5.39 \)

66. What is the test statistic?
   a) \( z = 2.542 \)
   b) \( t = 0.508 \)
   c) \( t = 2.542 \)
   d) \( z = 0.508 \)
67. What is the probability that the test statistic equals the observed value or a value even more extreme if the null hypothesis is true?
   a) b/t 0.01 and 0.005
   b) b/t 0.01 and 0.02
   c) .0180
   d) .9910

68. What is the 95% confidence interval for the population mean amount of radioactive byproducts?
   a) (5.07, 5.71)
   b) (5.00, 5.77)
   c) (5.09, 5.69)
   d) (4.92, 5.64)

69. What is the conclusion if you use significance level $\alpha = 0.05$?
   a) We fail to reject that the average radioactivity in the water is 5 pCi/L
   b) We fail to reject that the average radioactivity in the water is 5.39 pCi/L
   c) We have enough evidence to reject that the average radioactivity in the water is 5 pCi/L
   d) We have enough evidence to reject that the average radioactivity in the water is 5.39 pCi/L

70. What is the hypothesis for the McNemar test?
   a) Ho: $p_1 - p_2 = 0$, Ha: $p_1 - p_2 > 0$.
   b) Ho: $p_1 - p_2 = 0$, Ha: $p_1 - p_2 < 0$.
   c) Ho: $p_1 - p_2 = 0$, Ha: $p_1 - p_2 \neq 0$.
   d) Ho: $p = 0$, Ha: $p \neq 0$.
   e) Ho: $p = 0$, Ha: $p > 0$. 
71. What is the test statistic for the McNemar test for the table below?

<table>
<thead>
<tr>
<th></th>
<th>yes</th>
<th>no</th>
</tr>
</thead>
<tbody>
<tr>
<td>yes</td>
<td>a</td>
<td>b</td>
</tr>
<tr>
<td>no</td>
<td>c</td>
<td>d</td>
</tr>
</tbody>
</table>

a) Test Statistic = \( \frac{b + c}{b - c} \)

b) Test Statistic = \( \frac{a - d}{\sqrt{a + d}} \)

c) Test Statistic = \( \frac{b - c}{\sqrt{b + c}} \)

d) Test Statistic = \( \frac{a - b}{\sqrt{a + b}} \)

e) Test Statistic = \( \frac{a - d}{\sqrt{a + d}} \)

**Question 72 – 80** For a random sample of 1600 voting-age Americans, 944 people indicate approval of the President’s performance in office. A month later, 880 of these same 1600 people indicate approval. Table below shows the result.

<table>
<thead>
<tr>
<th>First Survey</th>
<th>Second Survey</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Approve</td>
<td>Disapprove</td>
</tr>
<tr>
<td>Approve</td>
<td>794</td>
<td>150</td>
</tr>
<tr>
<td>Disapprove</td>
<td>86</td>
<td>570</td>
</tr>
<tr>
<td>Total</td>
<td>880</td>
<td>720</td>
</tr>
</tbody>
</table>

72. Determine whether the sample is dependent or independent?
   a) Dependent.
   b) Independent.

73. What is the value of the test statistic?
   a) Test statistic = 5.25 or -5.25.
   b) Test statistic = 6.07 or -6.07.
   c) Test statistic = 4.17 or -4.17.
   d) Test statistic = 0.271 or – 0.271.
74. Give the conclusion for the test (take $\alpha = 0.05$)
   a) We reject the null and conclude that there is no significant evidence of the change in approval rating.
   b) We fail to reject the null and conclude that there is significant evidence of the change in the approval rating.
   c) We accept the null and conclude that there is significant evidence of the change in the approval rating.
   d) We reject the null and conclude that there is significant evidence of the change in approval rating.

75. In hypothesis testing, if you made a Type I error, you would do which of the following?
   a.) Reject Ho when Ho was True
   b.) Reject Ho when Ho was False
   c.) Fail to Reject Ho when Ho was True
   d.) Fail to Reject Ho when Ho was False

76. In hypothesis testing, if you made a Type II error, you would do which of the following?
   a.) Reject Ho when Ho was True
   b.) Reject Ho when Ho was False
   c.) Fail to Reject Ho when Ho was True
   d.) Fail to Reject Ho when Ho was False