

# STA 4211 – Exam 1 Take-Home Portion

Due at 10:40 AM 2/9/18

A manufacturer buys chemicals from three vendors (A,B,and C). You sample  $n_i=6$  units from each vendor and make an assessment of the purity of the sample. You fit the model:

$$Y_{ij} = \mu_i + \varepsilon_{ij} \quad \varepsilon_{ij} \sim NID(0, \sigma^2) \quad i = 1, 2, 3 \quad j = 1, \dots, 6$$

Complete the following parts:

- 1) Give unbiased estimates of all model parameters.

$$\hat{\mu}_1 = \text{_____} \quad \hat{\mu}_2 = \text{_____} \quad \hat{\mu}_3 = \text{_____} \quad s^2 = \text{_____}$$

- 2) Obtain the Analysis of Variance

Source	df	SS	MS	F*	F(.95)	P-value
Vendors						
Error						
Total						

- 3) Test whether there are differences among the three vendors ( $\alpha=0.05$ )

$$H_0 : \text{_____} \quad H_A : \text{_____}$$

Test Statistic: \_\_\_\_\_ Rejection Region: \_\_\_\_\_

Conclude (Circle One):    Reject  $H_0$     Fail to Reject  $H_0$

- 4) Give a contrast that compares vendor A with vendors B and C. Is vendor A's mean significantly different from the average of vendor's B and C at  $\alpha=0.05$  significance level? Conduct the F- test and obtain a confidence interval to make this decision.

$$H_0 : \text{_____} \quad H_A : \text{_____}$$

Test Statistic: \_\_\_\_\_ Rejection Region: \_\_\_\_\_

95% Confidence Interval: \_\_\_\_\_

Conclude (Circle One):    Reject  $H_0$     Fail to Reject  $H_0$

- 5) Obtain Simultaneous 95% CI's for the true differences in all pairs of treatment means based on Bonferroni's, Scheffe's, and Tukey's methods. Which pairs are significantly different based on each method?

Method	MSD	$\bar{y}_A - \bar{y}_B$	CI for $\mu_A - \mu_B$	$\bar{y}_A - \bar{y}_C$	CI for $\mu_A - \mu_C$	$\bar{y}_B - \bar{y}_C$	CI for $\mu_B - \mu_C$
Bonferroni							
Scheffe							
Tukey							

- 6) Test whether the population variances are equal, based on Bartlett's test with  $\alpha=0.05$ .

Test Statistic \_\_\_\_\_ Rejection Region \_\_\_\_\_